Taxing Wealth and Capital Income When Returns are Heterogeneous

Guvenen, Kambourov, Kuruscu, Ocampo

CEPR European Conference on Household Finance 2023

What is the optimal way to tax capital income (flow) and wealth (stock) when returns are heterogeneous?

What is the optimal way to tax capital income (flow) and wealth (stock) when returns are heterogeneous?

▶ If the return, r, is the same for all individuals, the two taxes are equivalent with $\tau_a = r\tau_k$.

What is the optimal way to tax capital income (flow) and wealth (stock) when returns are heterogeneous?

▶ If the return, r, is the same for all individuals, the two taxes are equivalent with $\tau_a = r\tau_k$.

Our earlier work: Quantitative analysis of optimal capital income versus wealth tax (Guvenen, Kambourov, Kuruscu, Ocampo, Chen, QJE 2023)

- ► Rich OLG model with return heterogeneity, bells & whistles
- ▶ Find: Large efficiency & welfare gains from replacing capital income tax with wealth tax

What is the optimal way to tax capital income (flow) and wealth (stock) when returns are heterogeneous?

▶ If the return, r, is the same for all individuals, the two taxes are equivalent with $\tau_a = r\tau_k$.

Our earlier work: Quantitative analysis of optimal capital income versus wealth tax (Guvenen, Kambourov, Kuruscu, Ocampo, Chen, QJE 2023)

- ► Rich OLG model with return heterogeneity, bells & whistles
- ▶ Find: Large efficiency & welfare gains from replacing capital income tax with wealth tax

This paper: Theoretical analysis of optimal combination of taxes

- ► Analytical model with workers, heterogeneous entrepreneurs, and innovation
- ► Find: conditions for (i) efficiency gains (ii) welfare effects (iii) optimal taxes (iv) effects on innovation

At least 4 reasons:

At least 4 reasons:

1. **Empirical:** A growing literature documents <u>persistent</u> return heterogeneity.

Bach, Calvet and Sodini 2020; Fagereng, Guiso, Malacrino, Pistaferri 2020; Smith, Yagan, Zidar, Zwick 2023

At least 4 reasons:

1. **Empirical:** A growing literature documents <u>persistent</u> return heterogeneity.

Bach, Calvet and Sodini 2020; Fagereng, Guiso, Malacrino, Pistaferri 2020; Smith, Yagan, Zidar, Zwick 2023

- 2. **Technical:** Capital taxes paid by the very wealthy.
 - Models struggle to generate plausible wealth inequality.

Guvenen, Kambourov, Kuruscu, Ocampo, Chen 2023

■ Return heterogeneity generates concentration at the very top, Pareto tail, and fast wealth growth Benhabib, Bisin, et al, 2011–2018; Gabaix, Lasry, Lions, Moll et al 2016; Jones, Kim 2018;

Pareto Tail vs. Models

At least 4 reasons:

1. **Empirical:** A growing literature documents persistent return heterogeneity.

Bach, Calvet and Sodini 2020; Fagereng, Guiso, Malacrino, Pistaferri 2020; Smith, Yagan, Zidar, Zwick 2023

- 2. **Technical:** Capital taxes paid by the very wealthy.
 - Models struggle to generate plausible wealth inequality.
 - Return heterogeneity generates concentration at the very top, Pareto tail, and fast wealth growth Benhabib, Bisin, et al, 2011–2018; Gabaix, Lasry, Lions, Moll et al 2016; Jones, Kim 2018; Guvenen, Kambourov, Kuruscu, Ocampo, Chen 2023

Pareto Tail vs. Models

- 3. Practical: Wealth taxation has been used by governments
 - We need to provide better guidance to policy makers.

At least 4 reasons:

1. **Empirical:** A growing literature documents <u>persistent</u> return heterogeneity.

Bach, Calvet and Sodini 2020; Fagereng, Guiso, Malacrino, Pistaferri 2020; Smith, Yagan, Zidar, Zwick 2023

- 2. **Technical:** Capital taxes paid by the very wealthy.
 - Models struggle to generate plausible wealth inequality.
 - Return heterogeneity generates concentration at the very top, Pareto tail, and fast wealth growth Benhabib, Bisin, et al, 2011–2018; Gabaix, Lasry, Lions, Moll et al 2016; Jones, Kim 2018; Guvenen, Kambourov, Kuruscu, Ocampo, Chen 2023

Pareto Tail vs. Models

- 3. Practical: Wealth taxation has been used by governments
 - We need to provide better guidance to policy makers.
- Theoretical: Interesting new economic mechanisms → Example next.
 Allais 1977, Piketty 2014, Guvenen, Kambourov, Kuruscu, Ocampo, Chen 2023

Return Heterogeneity: A Simple Example

- ► One-period model.
- ▶ Government taxes to finance G = \$50K.
- ► Two brothers, Fredo and Mike, each with \$1M of wealth.

Return Heterogeneity: A Simple Example

- One-period model.
- ▶ Government taxes to finance G = \$50K.
- ► Two brothers, Fredo and Mike, each with \$1M of wealth.
- ► Key heterogeneity: investment/entrepreneurial ability.
 - (Fredo) Low ability: earns $r_f = 0\%$ rate of return.
 - (Mike) High ability: earns $r_m = 20\%$ rate of return.

	Capital income tax		Wealth tax
	$a_{i, \text{after-tax}} = a_i + (1 - \tau_k) r_i a_i$		
	Fredo $(r_f = 0\%)$	Mike $(r_m = 20\%)$	
Wealth	\$1M	\$1M	
Before-tax Income	\$0	\$200K	
Tax liability			
After-tax return			
After-tax wealth ratio			

	Capital income tax		Wealth tax
	$a_{i, ext{after-tax}} = a_i + rac{(1- au_k)}{r_i a_i}$		
	Fredo $(r_f = 0\%)$	Mike (<i>r_m</i> = 20%)	
Wealth	\$1M	\$1M	
Before-tax Income	\$0	\$200K	
	$\tau_k = 259$	$\frac{6}{6} \left(= \frac{50}{200} \right)$	
Tax liability	0	\$50K (= $200\tau_k$)	
After-tax return			
After-tax wealth ratio			

	Capital i	ncome tax	Wealth tax
	$a_{i,after-tax} = a$	$r_i + (1 - \tau_k)r_i a_i$	
	Fredo $(r_f = 0\%)$	Mike (<i>r_m</i> = 20%)	
Wealth	\$1M	\$1M	
Before-tax Income	\$0	\$200K	
	$\tau_k = 25$	$\frac{2}{6} \left(= \frac{50}{200} \right)$	
Tax liability	0	\$50K (= $200\tau_k$)	
After-tax return	0%	$15\% \left(= \frac{200 - 50}{1000} \right)$	
After-tax wealth ratio	1.15 (=	1150/1000)	

	Capital income tax $a_{i,\text{after-tax}} = a_i + (1 - \tau_k)r_i a_i$		Wealth tax (on book value)
			$a_{i, \text{after-tax}} = (1 - \tau_a)a_i + r_i a_i$
	Fredo $(r_f = 0\%)$	Mike (<i>r_m</i> = 20%)	
Wealth	\$1M	\$1M	
Before-tax Income	\$0	\$200K	
	$\tau_k = 25^{\circ}$	$\frac{2}{6} \left(= \frac{50}{200} \right)$	
Tax liability	0	\$50K (= $200\tau_k$)	
After-tax return	0%	$15\% \left(= \frac{200 - 50}{1000} \right)$	
After-tax wealth ratio	1.15 (=	1150/1000)	

	Capital income tax $a_{i,\text{after-tax}} = a_i + (1 - \tau_k)r_i a_i$		Wealth tax (on book value) $a_{i, ext{after-tax}} = (1 - au_a)a_i + r_i a_i$	
	Fredo $(r_f = 0\%)$	Mike $(r_m = 20\%)$	Fredo $(r_f = 0\%)$	Mike $(r_m = 20\%)$
Wealth	\$1M	\$1M	\$1M	\$1M
Before-tax Income	\$0	\$200K	0	\$200K
	$\tau_k = 25^{\circ}$	$\frac{2}{6} \left(= \frac{50}{200} \right)$		
Tax liability	0	\$50K (= $200 au_k$)		
After-tax return	0%	$15\% \left(= \frac{200 - 50}{1000} \right)$		
After-tax wealth ratio	1.15 (=	1150/1000)		

	Capital income tax $a_{i, ext{after-tax}} = a_i + (1 - au_k) r_i a_i$		Wealth tax (d	on book value)
			$a_{i,after-tax} = ig(1 - au_{a}ig)a_i + r_i a_i$	
	Fredo $(r_f = 0\%)$	Mike $(r_m = 20\%)$	Fredo ($r_f = 0\%$)	Mike $(r_m = 20\%)$
Wealth	\$1M	\$1M	\$1M	\$1M
Before-tax Income	\$0	\$200K	0	\$200K
	$\tau_k = 25^{\circ}$	$\frac{50}{200}$ (= $\frac{50}{200}$)	$ au_a = 2.5\% \left(= \frac{50}{2000} \right)$	
Tax liability	0	\$50K (= $200 au_k$)	$$25 \mathrm{K} \ (= 1000 \tau_a)$	$25 \mathrm{K} \ (= 1000 \tau_a)$
After-tax return After-tax wealth ratio	0% 1.15 (=	$15\% \left(= \frac{200 - 50}{1000} \right)$ $^{1150}/_{1000}$		

	Capital income tax $a_{i, ext{after-tax}} = a_i + (1 - au_k) r_i a_i$			on book value)
			$a_{i,\text{after-tax}} = \frac{(1 - \tau_a)a_i + r_i a_i}{1 - \tau_a}$	
	Fredo ($r_f = 0\%$)	Mike ($r_m = 20\%$)	Fredo ($r_f = 0\%$)	Mike $(r_m = 20\%)$
Wealth	\$1M	\$1M	\$1M	\$1M
Before-tax Income	\$0	\$200K	0	\$200K
	$\tau_k = 25$	$\frac{2}{6} \left(= \frac{50}{200} \right)$	$\tau_a = 2.5\% \left(= \frac{50}{2000} \right)$	
Tax liability	0	\$50K (= $200\tau_k$)	$$25 \mathrm{K} \ (= 1000 \tau_a)$	$25 \text{K} (= 1000 \tau_a)$
After-tax return After-tax wealth ratio	0% 1.15 (=	$15\% \left(= \frac{200 - 50}{1000} \right)$ $1150/1000)$	$-2.5\% \left(=\frac{0-25}{1000}\right)$ $\frac{1.20}{1.20} \left(\approx\right)$	$17.5\% \left(=\frac{200-25}{1000}\right)$ 1175/975)

	Capital i	ncome tax	Wealth tax (o	n book value)
	$a_{i, ext{after-tax}} = a_i + rac{\left(1 - au_k ight) r_i a_i}{2}$		$a_{i, ext{after-tax}} = (1- au_{ ext{a}})a_i + r_i a_i$	
	Fredo $(r_f = 0\%)$	Mike $(r_m = 20\%)$	Fredo ($r_f = 0\%$)	Mike $(r_m = 20\%)$
Wealth	\$1M	\$1M	\$1M	\$1M
Before-tax Income	\$0	\$200K	0	\$200K
	$\tau_k = 25\% \left(= \frac{50}{200} \right)$		$\tau_a = 2.5\% \left(= \frac{50}{2000} \right)$	
Tax liability	0	\$50K (= $200 au_k$)	$$25 \mathrm{K} \ (= 1000 \tau_a)$	$25 \mathrm{K} \ (= 1000 \tau_a)$
After-tax return After-tax wealth ratio	0% 1.15 (=	$15\% \left(= \frac{200 - 50}{1000} \right)$ $1150/1000)$	$-2.5\% \left(=\frac{0-25}{1000}\right)$ $\frac{1.20}{1.20} \left(\approx\right)$	(1000 /

Replacing τ_k with $\tau_a \to \text{reallocates}$ capital to more productive agent (use it or lose it) \to TFP \uparrow

	Capital i	ncome tax	Wealth tax (c	Wealth tax (on book value)	
	$a_{i, ext{after-tax}} = a_i + \left(1 - au_k ight) r_i a_i$		$a_{i, ext{after-tax}} = (1- au_{ ext{a}})a_i + r_i a_i$		
	Fredo $(r_f = 0\%)$	Mike $(r_m = 20\%)$	Fredo ($r_f = 0\%$)	Mike $(r_m = 20\%)$	
Wealth	\$1M	\$1M	\$1M	\$1M	
Before-tax Income	\$0	\$200K	0	\$200K	
	$\tau_k = 25\% \left(= \frac{50}{200} \right)$		$ au_a = 2.5\% \left(= \frac{50}{2000} \right)$		
Tax liability	0	\$50K (= $200\tau_k$)	$$25 \mathrm{K} \ (= 1000 \tau_a)$	$25 \mathrm{K} \ (= 1000 \tau_a)$	
After-tax return	0%	$15\% \left(= \frac{200 - 50}{1000} \right)$	$-2.5\% \left(=\frac{0-25}{1000}\right)$	$17.5\% \left(=\frac{200-25}{1000}\right)$	
After-tax wealth ratio	1.15 (=	1150/1000)	1.20 (≈	1175/975)	

Replacing τ_k with $\tau_a \to \text{reallocates}$ capital to more productive agent (use it or lose it) \to TFP \uparrow + increases dispersion in after-tax returns & wealth.

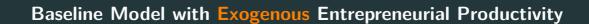
	Capital i	ncome tax	Wealth tax (on book value)	
	$a_{i, ext{after-tax}} = a_i + \frac{(1 - au_k)r_i a_i}{}$		$a_{i, ext{after-tax}} = (1- au_{ ext{a}})a_i + r_i a_i$	
	Fredo $(r_f = 0\%)$	Mike $(r_m = 20\%)$	Fredo ($r_f = 0\%$)	Mike $(r_m = 20\%)$
Wealth	\$1M	\$1M	\$1M	\$1M
Before-tax Income	\$0	\$200K	0	\$200K
	$ au_k = 25\% \left(= \frac{50}{200} \right)$		$\tau_a = 2.5\% \left(= \frac{50}{2000} \right)$	
Tax liability	0	\$50K (= $200 au_k$)	$$25 \mathrm{K} \ (= 1000 \tau_a)$	$25 \mathrm{K} \ (= 1000 \tau_a)$
After-tax return After-tax wealth ratio	0% 1.15 (=	$15\% \ (= \frac{200 - 50}{1000})$ $1150/1000)$	(1000 /	$17.5\% \left(=\frac{200-25}{1000}\right)$ $1175/975)$

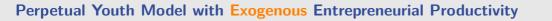
Use it or lose it effect relies on taxing book value.

	Capital i	ncome tax	Wealth tax (c	on book value)
	$a_{i, ext{after-tax}} = a_i + (1 - au_k) r_i a_i$		$a_{i,after-tax} = ig(1 - au_{a}ig)a_i + r_i a_i$	
	Fredo $(r_f = 0\%)$	Mike $(r_m = 20\%)$	Fredo ($r_f = 0\%$)	Mike ($r_m = 20\%$)
Wealth Before-tax Income	\$1M \$ 0	\$1M \$ 200K	\$1M 0	\$ 1M \$200K
	$\tau_k = 25^{\circ}$	$\frac{50}{200}$ (= $\frac{50}{200}$)	$\tau_a = 2.5\% \left(= \frac{50}{2000} \right)$	
Tax liability	0	\$50K (= $200\tau_k$)	$$25 \mathrm{K} \ (= 1000 \tau_a)$	$25K (= 1000\tau_a)$
After-tax return After-tax wealth ratio	0% 1.15 (=	$15\% \left(= \frac{200 - 50}{1000} \right)$ $^{1150}/_{1000})$	(1000 /	17.5% (= $\frac{200-25}{1000}$) 1175/975)

Use it or lose it effect relies on taxing book value.

In contrast, market value reflects productivity \rightarrow taxing it has a limited **use it or lose it** effect.





- 1. Homogenous workers (size *L*)
 - $\blacksquare \ \, \mathsf{Supply} \ \, \mathsf{labor} \ \, \mathsf{inelastically} + \mathsf{consume} \ \, \mathsf{wage} \ \, \mathsf{income} \ \, (\mathit{hand-to-mouth})$

- 1. Homogenous workers (size *L*)
 - Supply labor inelastically + consume wage income (hand-to-mouth)
- 2. Heterogenous entrepreneurs (size 1)
 - Produce final goods using capital and labor $(y_i = (z_i k_i)^{\alpha} n_i^{1-\alpha}) + \text{consume/save}$
 - Heterogeneity in
 - ▶ productivity $(z_i \in \{z_\ell, z_h\})$ determined at birth: μ (1μ) fraction w/ permanent z_h (z_ℓ)
 - ▶ wealth (a)
 - Initial (inherited) wealth a common across entrepreneurs (a determined endogenously later)

- 1. Homogenous workers (size L)
 - Supply labor inelastically + consume wage income (hand-to-mouth)
- 2. Heterogenous entrepreneurs (size 1)
 - Produce final goods using capital and labor $(y_i = (z_i k_i)^{\alpha} n_i^{1-\alpha}) + \text{consume/save}$
 - Heterogeneity in
 - ▶ productivity $(z_i \in \{z_\ell, z_h\})$ determined at birth: μ (1μ) fraction w/ permanent z_h (z_ℓ)
 - ▶ wealth (a)
 - Initial (inherited) wealth a common across entrepreneurs (a determined endogenously later)

Preferences (of workers and entrepreneurs): $E_0 \sum_{t=0}^{\infty} (\beta \delta)^t \log(c_t)$

where $\beta < 1$ and $\delta < 1$ is the conditional survival probability.

- 1. Homogenous workers (size *L*)
 - Supply labor inelastically + consume wage income (hand-to-mouth)
- 2. Heterogenous entrepreneurs (size 1)
 - Produce final goods using capital and labor $(y_i = (z_i k_i)^{\alpha} n_i^{1-\alpha}) + \text{consume/save}$
 - Heterogeneity in
 - ▶ productivity $(z_i \in \{z_\ell, z_h\})$ determined at birth: μ (1μ) fraction w/ permanent z_h (z_ℓ)
 - ▶ wealth (a)
 - Initial (inherited) wealth a common across entrepreneurs (a determined endogenously later)

Preferences (of workers and entrepreneurs): $E_0 \sum_{t=0}^{\infty} (\beta \delta)^t \log(c_t)$

where $\beta < 1$ and $\delta < 1$ is the conditional survival probability.

Aggregate output: $Y = \int y_i di = \int (z_i k_i)^{\alpha} n_i^{1-\alpha} di$

Government: Finances exogenous expenditure G with τ_k and τ_a

Financial Markets & Equilibrium with Heterogenous Returns

Financial markets:

- ► Collateral constraint $(\lambda > 1)$: $k \le \lambda a$, where a is entrepreneur's wealth.
- ► Bonds are in zero net supply.

Financial Markets & Equilibrium with Heterogenous Returns

Financial markets:

- ► Collateral constraint $(\lambda > 1)$: $k \le \lambda a$, where a is entrepreneur's wealth.
- ▶ Bonds are in zero net supply.

Equilibrium with Heterogenous Returns:

- ▶ If $\mu(\lambda 1) A_h < (1 \mu) A_\ell$:
 - low-type entrepreneurs bid down interest rate, $r = MPK(z_{\ell})$.
 - Unique steady state with: return heterogeneity, misallocation of capital, wealth tax \neq capital income tax.
 - Empirically relevant: $R_h > R_l$ and $\frac{\text{Debt}}{\text{GDP}} \gg 1.5$ when $\lambda = \overline{\lambda}$.

Financial Markets & Equilibrium with Heterogenous Returns

Financial markets:

- ► Collateral constraint $(\lambda > 1)$: $k \le \lambda a$, where a is entrepreneur's wealth.
- ▶ Bonds are in zero net supply.

Equilibrium with Heterogenous Returns:

- ▶ If $\mu(\lambda 1) A_h < (1 \mu) A_\ell$:
 - low-type entrepreneurs bid down interest rate, $r = MPK(z_{\ell})$.
 - Unique steady state with: return heterogeneity, misallocation of capital, wealth tax \neq capital income tax.
 - Empirically relevant: $R_h > R_l$ and $\frac{\text{Debt}}{\text{GDP}} \gg 1.5$ when $\lambda = \overline{\lambda}$.

$$\blacktriangleright \mu(\lambda - 1) A_h < (1 - \mu) A_\ell \longleftrightarrow \tau_{\mathsf{a}} < \overline{\tau}_{\mathsf{a}} = 1 - \frac{1}{\beta \delta} \left(1 - \frac{1 - \delta}{\delta} \frac{1 - \lambda \mu}{(\lambda - 1) \left(1 - \frac{z_\ell}{z_k} \right)} \right)$$



Equilibrium Values: Aggregation

Lemma: Aggregate output is

$$Y = (ZK)^{\alpha} L^{1-\alpha}$$
 (Z^{α} is measured TFP)

where

$$K \equiv \mu A_h + (1 - \mu) A_\ell$$

$$Z \equiv s_h z_\lambda + (1 - s_h) z_\ell$$

$$K = Aggregate capital$$

$$Z = Wealth-weighted productivity$$

Equilibrium Values: Aggregation

Lemma: Aggregate output is

$$Y = (ZK)^{\alpha} L^{1-\alpha}$$
 (Z^{α} is measured TFP)

where

$$K \equiv \mu \, A_h + (1 - \mu) \, A_\ell$$
 $K =$ Aggregate capital $Z \equiv s_h \, z_\lambda \, + \, (1 - s_h) \, z_\ell$ $Z =$ Wealth-weighted productivity

Key variables:

- $s_h = \frac{\mu A_h}{K}$: wealth share of high-productivity entrepreneurs.
- ightharpoonup $z_{\lambda} \equiv z_h + (\lambda 1)(z_h z_{\ell})$: effective productivity of high-productivity entrepreneurs.

Use it or lose it effect increases efficiency if $s_h \uparrow (\longrightarrow Z \uparrow)$

Steady State: Capital, Returns, and Taxes

Steady State K: Same as in Neoclassical Growth Model... but with endogenous Z (Moll, 2014)

$$(1 - \tau_a) + (1 - \tau_k) \overbrace{\alpha Z^{\alpha} (\kappa/\iota)^{\alpha - 1}}^{\text{MPK}} = \frac{1}{\beta \delta}$$

Steady State: Capital, Returns, and Taxes

Steady State K: Same as in Neoclassical Growth Model... but with endogenous Z (Moll, 2014)

$$(1 - \tau_k) \overbrace{\alpha Z^{\alpha} (K/L)^{\alpha - 1}}^{\text{MPK}} = \frac{1}{\beta \delta} - (1 - \tau_a)$$

 $ightharpoonup au_k$ does not affect steady state after-tax MPK; au_a does.

Steady State: Capital, Returns, and Taxes

Steady State K: Same as in Neoclassical Growth Model... but with endogenous Z (Moll, 2014)

$$(1-\tau_k)\overbrace{\alpha^{Z^{\alpha}}(^{K}/L)^{\alpha-1}}^{\text{MPK}} = \frac{1}{\beta\delta} - (1-\tau_a)$$

 $ightharpoonup au_k$ does not affect steady state after-tax MPK; au_a does.

Steady State *Z*: Returns and evolution of assets imply this quadratic equation:

$$(1 - \delta^{2}\beta (1 - \tau_{a})) Z^{2} - [(1 - \delta) (\mu z_{\lambda} + (1 - \mu) z_{\ell}) + \delta (1 - \delta\beta (1 - \tau_{a})) (z_{\lambda} + z_{\ell})] Z$$

$$+ \delta (1 - \delta\beta (1 - \tau_{a})) z_{\ell} z_{\lambda} = 0.$$

ightharpoonup Z only depends on τ_a .

Steady State: Capital, Returns, and Taxes

Steady State K: Same as in Neoclassical Growth Model... but with endogenous Z (Moll, 2014)

$$(1-\tau_k)\overbrace{\alpha^{Z^{\alpha}}(^{K}/L)^{\alpha-1}}^{\text{MPK}} = \frac{1}{\beta\delta} - (1-\tau_a)$$

 $ightharpoonup au_k$ does not affect steady state after-tax MPK; au_a does.

Steady State *Z*: Returns and evolution of assets imply this quadratic equation:

$$(1 - \delta^{2}\beta (1 - \tau_{a})) Z^{2} - [(1 - \delta) (\mu z_{\lambda} + (1 - \mu) z_{\ell}) + \delta (1 - \delta\beta (1 - \tau_{a})) (z_{\lambda} + z_{\ell})] Z$$

$$+ \delta (1 - \delta\beta (1 - \tau_{a})) z_{\ell} z_{\lambda} = 0.$$

- ightharpoonup Z only depends on τ_a .
- ▶ Wealth tax affects returns, wealth shares, and productivity. Capital income tax does not.

Steady State: Capital, Returns, and Taxes

Steady State K: Same as in Neoclassical Growth Model... but with endogenous Z (Moll, 2014)

$$(1-\tau_k)\overbrace{\alpha^{Z^{\alpha}}(^{K}/L)^{\alpha-1}}^{\text{MPK}} = \frac{1}{\beta\delta} - (1-\tau_a)$$

ightharpoonup does not affect steady state after-tax MPK; τ_a does.

Steady State *Z*: Returns and evolution of assets imply this quadratic equation:

$$(1 - \delta^{2}\beta (1 - \tau_{a})) Z^{2} - [(1 - \delta) (\mu z_{\lambda} + (1 - \mu) z_{\ell}) + \delta (1 - \delta\beta (1 - \tau_{a})) (z_{\lambda} + z_{\ell})] Z$$

$$+ \delta (1 - \delta\beta (1 - \tau_{a})) z_{\ell} z_{\lambda} = 0.$$

- ightharpoonup Z only depends on τ_a .
- Wealth tax affects returns, wealth shares, and productivity. Capital income tax does not.
- ▶ **Note:** Both taxes affect capital, output, wages...

Main Result 1: Efficiency Gains from Wealth Taxation

Proposition:

Proof

For all $\mu \in (0,1)$ and $\tau_a < \overline{\tau}_a$, an increase in τ_a increases Z

Main Result 1: Efficiency Gains from Wealth Taxation

Proposition:

Proof

For all $\mu \in (0,1)$ and $\tau_a < \bar{\tau}_a$, an increase in τ_a increases **Z**

Corollary: For all $\mu \in (0,1)$ and $\tau_a < \bar{\tau}_a$, an increase in τ_a increases

▶ Wealth concentration: $s_h \uparrow (Z \uparrow = s_h z_\lambda + (1 - s_h) z_\ell)$

Main Result 1: Efficiency Gains from Wealth Taxation

Proposition:

For all $\mu \in (0,1)$ and $\tau_a < \bar{\tau}_a$, an increase in τ_a increases Z

Corollary: For all $\mu \in (0,1)$ and $\tau_a < \bar{\tau}_a$, an increase in τ_a increases

- ▶ Wealth concentration: $s_h \uparrow (Z \uparrow = s_h z_\lambda + (1 s_h) z_\ell)$
- ► Dispersion of after-tax returns rises:

$$\frac{dR_{\ell}}{d\tau_a} < \mathbf{0} \qquad \& \qquad \frac{dR_h}{d\tau_a} > \mathbf{0}$$

Proof

Government Budget and Aggregate Variables

$$G = \tau_k \alpha Y + \tau_a K$$
.

▶ In what follows, τ_k adjusts in the background when $\tau_a \uparrow$

Government Budget and Aggregate Variables

$$G = \tau_k \alpha Y + \tau_a K$$
.

▶ In what follows, τ_k adjusts in the background when $\tau_a \uparrow$

Lemma:

For all $\mu \in (0,1)$ and $\tau_a < \overline{\tau}_a$, an increase in τ_a has the following effect on aggregates:

▶ Increases capital (K), output (Y), wage (W), & h-type wealth (A_h)

Government Budget and Aggregate Variables

$$G = \tau_k \alpha Y + \tau_a K$$
.

▶ In what follows, τ_k adjusts in the background when $\tau_a \uparrow$

Lemma:

For all $\mu \in (0,1)$ and $\tau_a < \overline{\tau}_a$, an increase in τ_a has the following effect on aggregates:

- ▶ Increases capital (K), output (Y), wage (w), & h-type wealth (A_h)
- **Key:** Higher $\alpha \longrightarrow \text{Larger pass-through of TFP to } \textit{K, Y, w}$

$$\xi_K = \xi_Y = \xi_w = \alpha/1-\alpha$$
 $\xi_X = \frac{d \log X}{d \log Z}$

Main Result 2: Welfare Gains by Type

Proposition:

For all $\tau_a < \overline{\tau}_a$, a higher τ_a changes welfare as follows:

- lacktriangle Workers: Higher welfare: $rac{dV_{workers}}{d au_a}>0$
- ▶ High-z entrepreneurs: Higher welfare: $\frac{dV_h(\bar{a})}{d\tau_a} > 0$ (since $\xi_K + \frac{1}{1-\beta\delta}\xi_{R_h} > 0$)
- ▶ Low-z entrepreneurs: Lower welfare $\left(\frac{dV_{\ell}(\bar{a})}{d\tau_a} < 0\right)$ iff $\xi_K + \frac{1}{1-\beta\delta}\xi_{R_{\ell}} < 0$
- ► Entrepreneurs: Lower average welfare iff $\xi_K + \frac{1}{1-\beta\delta} \left(\mu \xi_{R_h} + (1-\mu) \xi_{R_\ell} \right) < 0$

Main Result 2: Welfare Gains by Type

Proposition:

For all $\tau_a < \overline{\tau}_a$, a higher τ_a changes welfare as follows:

- ▶ Workers: Higher welfare: $\frac{dV_{workers}}{d\tau_a} > 0$
- ▶ High-z entrepreneurs: Higher welfare: $\frac{dV_h(\bar{a})}{d\tau_a} > 0$ (since $\xi_K + \frac{1}{1-\beta\delta}\xi_{R_h} > 0$)
- ▶ Low-z entrepreneurs: Lower welfare $\left(\frac{dV_{\ell}(\overline{a})}{d\tau_a} < 0\right)$ iff $\xi_K + \frac{1}{1-\beta\delta}\xi_{R_{\ell}} < 0$
- ► Entrepreneurs: Lower average welfare iff $\xi_K + \frac{1}{1-\beta\lambda} \left(\mu \xi_{R_h} + (1-\mu) \xi_{R_\ell} \right) < 0$

Note: The last two conditions imply a threshold on α for welfare gains that are high in practice, so average entrepreneur welfare is typically lowered when τ_a increases.

 α Thresholds

Main Result 3: Optimal Taxes



Objective: Choose taxes (τ_a, τ_k) to maximize newborn welfare

$$\mathcal{W} \equiv n_{w}V_{w}(w) + (1 - n_{w})\left(\mu V_{h}(\overline{a}) + (1 - \mu)V_{\ell}(\overline{a})\right)$$

Main Result 3: Optimal Taxes



Objective: Choose taxes (τ_a, τ_k) to maximize newborn welfare

$$\mathcal{W} = \frac{1}{1 - \beta \delta} \left\{ n_w \log w + (1 - n_w) \left(\log \overline{a} + \frac{\mu \log R_h + (1 - \mu) \log R_\ell}{1 - \beta \delta} \right) \right\} + \text{Constant}$$

Main Result 3: Optimal Taxes



Objective: Choose taxes (τ_a, τ_k) to maximize newborn welfare

$$\mathcal{W} = \frac{1}{1 - \beta \delta} \left\{ n_w \log w + (1 - n_w) \left(\log \overline{a} + \frac{\mu \log R_h + (1 - \mu) \log R_\ell}{1 - \beta \delta} \right) \right\} + \mathsf{Constant}$$

Proposition: There exists a unique optimal tax combination (τ_a^*, τ_k^*) that maximizes \mathcal{W} . An interior optimum $(\tau_a^* < \bar{\tau}_a)$ is the solution to:

$$0 = \left(\underbrace{n_w \xi_w^Z + (1 - n_w) \xi_K^Z}_{\text{Level Effect (+)} = \frac{\alpha}{1 - \alpha}} + \underbrace{\frac{1 - n_w}{1 - \beta \delta} \left(\mu \xi_{R_h}^Z + (1 - \mu) \xi_{R_\ell}^Z\right)}_{\text{Return Productivity Effect (-)}}\right) \frac{d \log Z}{d \tau_a}$$

where $\xi_x \equiv \frac{d \log x}{d \log Z}$ is the elasticity of variable x with respect to Z. **Furthermore**,

$$\begin{split} \tau_a^\star < &0 \text{ and } \tau_k^\star > 0 \\ \tau_a^\star > &0 \text{ and } \tau_k^\star > 0 \end{split} \qquad \qquad &\text{if } \alpha < \underline{\alpha} \\ \text{if } \underline{\alpha} \leq \underline{\alpha} \leq \bar{\alpha} \\ \tau_a^\star > &0 \text{ and } \tau_k^\star < 0 \end{cases}$$

How the Optimal Wealth Tax Varies with β and productivity dispersion

0.1

0.96 ↓



 $\textbf{Figure 1:} \ \, \mathsf{Optimal} \ \, \mathsf{Wealth} \ \, \mathsf{Tax}$

Note: The figure reports the value of the optimal wealth tax for combinations of the discount factor (β) and productivity dispersion ($^{z}\ell/z_{h}$). We set the remaining parameters as follows: $\delta = ^{49}/\text{so}$, $\beta \delta = 0.96$, $\mu = 0.10$, $z_{h} = 1$, $\tau_{k} = 25\%$, and $\alpha = 0.4$.

0.2 0.3 Productivity Ratio (z_l/z_h)

0.4

0.5

Baseline Model with Innovation and Endogenous Entrepreneurial Productivity

- \blacktriangleright We interpret productivity z_i as the outcome of a risky innovation process
- ▶ Innovation requires costly effort, e, and can end with a high-productivity idea if successful

Innovator's problem:

$$\max_{e} \ \mu\left(e\right) V_{h}\left(\overline{a}\right) + \left(1 - \mu(e)\right) \ V_{\ell}\left(\overline{a}\right) - \frac{1}{\left(1 - \beta\delta\right)^{2}} \Lambda\left(e\right); \quad \Lambda\left(e\right) \ \text{convex} + \mathcal{C}^{2}; \ \mu\left(e\right) = e$$

- \blacktriangleright We interpret productivity z_i as the outcome of a risky innovation process
- ▶ Innovation requires costly effort, e, and can end with a high-productivity idea if successful

Innovator's problem:

$$\max_{e} \ \mu\left(e\right) V_{h}\left(\overline{a}\right) + \left(1 - \mu(e)\right) \ V_{\ell}\left(\overline{a}\right) - \frac{1}{\left(1 - \beta\delta\right)^{2}} \Lambda\left(e\right); \quad \Lambda\left(e\right) \ \text{convex} + C^{2}; \ \mu\left(e\right) = e$$

We can show:

▶ Unique equilibrium with innovation. Efficiency gains with wealth tax. Same as before.

- \blacktriangleright We interpret productivity z_i as the outcome of a risky innovation process
- ▶ Innovation requires costly effort, e, and can end with a high-productivity idea if successful

Innovator's problem:

$$\max_{e} \ \mu\left(e\right) V_{h}\left(\overline{a}\right) + \left(1 - \mu(e)\right) \ V_{\ell}\left(\overline{a}\right) - \frac{1}{\left(1 - \beta\delta\right)^{2}} \Lambda\left(e\right); \quad \Lambda\left(e\right) \ \text{convex} + C^{2}; \ \mu\left(e\right) = e$$

We can show:

- ▶ Unique equilibrium with innovation. Efficiency gains with wealth tax. Same as before.
- ► Wealth tax increases innovation, hence fraction of high-type entrepreneurs.

- \blacktriangleright We interpret productivity z_i as the outcome of a risky innovation process
- ▶ Innovation requires costly effort, e, and can end with a high-productivity idea if successful

Innovator's problem:

$$\max_{e} \ \mu\left(e\right) V_{h}\left(\overline{a}\right) + \left(1 - \mu(e)\right) \ V_{\ell}\left(\overline{a}\right) - \frac{1}{\left(1 - \beta\delta\right)^{2}} \Lambda\left(e\right); \quad \Lambda\left(e\right) \ \text{convex} + C^{2}; \ \mu\left(e\right) = e$$

We can show:

- ▶ Unique equilibrium with innovation. Efficiency gains with wealth tax. Same as before.
- ► Wealth tax increases innovation, hence fraction of high-type entrepreneurs.
- ► Optimal wealth tax is higher.

Steady State μ^* : For a given wealth tax level $\tau_a \leq \overline{\tau}_a$, the steady state share of high-productivity entrepreneurs, μ^* , is determined by the solution to

$$\mu^{\star} = e(Z(\mu^{\star}))$$
, where

- i. $Z(\mu)$ gives the steady state productivity given μ .
- ii. e(Z) gives the optimal innovation effort given steady state productivity Z.

Steady State μ^* : For a given wealth tax level $\tau_a \leq \overline{\tau}_a$, the steady state share of high-productivity entrepreneurs, μ^* , is determined by the solution to

$$\mu^{\star} = e(Z(\mu^{\star}))$$
, where

- i. $Z(\mu)$ gives the steady state productivity given μ .
- ii. e(Z) gives the optimal innovation effort given steady state productivity Z.

Proposition (existence and uniqueness):

There exists a unique innovation equilibrium.

Steady State μ^* : For a given wealth tax level $\tau_a \leq \overline{\tau}_a$, the steady state share of high-productivity entrepreneurs, μ^* , is determined by the solution to

$$\mu^{\star} = e(Z(\mu^{\star}))$$
, where

- i. $Z(\mu)$ gives the steady state productivity given μ .
- ii. e(Z) gives the optimal innovation effort given steady state productivity Z.

Proposition (existence and uniqueness):

There exists a unique innovation equilibrium.

Proposition (innovation gains from wealth taxation):

The equilibrium μ^* is increasing in wealth taxes, τ_a .

Steady State μ^* : For a given wealth tax level $\tau_a \leq \overline{\tau}_a$, the steady state share of high-productivity entrepreneurs, μ^* , is determined by the solution to

$$\mu^{\star} = e(Z(\mu^{\star}))$$
, where

- i. $Z(\mu)$ gives the steady state productivity given μ .
- ii. e(Z) gives the optimal innovation effort given steady state productivity Z.

Proposition (existence and uniqueness):

There exists a unique innovation equilibrium.

Proposition (innovation gains from wealth taxation):

The equilibrium μ^{\star} is increasing in wealth taxes, τ_{a} .

Corollary (efficiency gains from wealth taxation):

The equilibrium Z^* is increasing in τ_a (+ Both μ^* and Z^* are independent of τ_k).

Optimal taxes with innovation

Objective: Choose $(\tau_a^{\star}, \tau_k^{\star})$ to maximize newborn welfare net of innovation costs

$$\mathcal{W} \equiv n_w V_w \left(w\right) + \left(1 - n_w\right) \left(\mu V_h \left(\overline{a}\right) + \left(1 - \mu\right) V_\ell \left(\overline{a}\right) - \frac{\Lambda \left(\mu\right)}{\left(1 - \beta \delta\right)^2}\right)$$

Optimal taxes with innovation

Objective: Choose $(\tau_a^{\star}, \tau_k^{\star})$ to maximize newborn welfare net of innovation costs

$$\mathcal{W} \equiv n_{w}V_{w}\left(w\right) + \left(1 - n_{w}\right)\left(\mu V_{h}\left(\overline{a}\right) + \left(1 - \mu\right)V_{\ell}\left(\overline{a}\right) - \frac{\Lambda\left(\mu\right)}{\left(1 - \beta\delta\right)^{2}}\right)$$

Proposition:

The optimal tax combination $(\tau_a^{\star}, \tau_k^{\star})$ that maximizes \mathcal{W} is the solution to:

$$0 = \left(\underbrace{\frac{n_w \xi_w^Z + (1 - n_w) \xi_K^Z}{\text{Level Effect (+)}}}_{\text{Level Effect (+)}} + \underbrace{\frac{1 - n_w}{1 - \beta \delta} \left(\mu \xi_{R_h}^Z + (1 - \mu) \xi_{R_\ell}^Z\right)}_{\text{Return Productivity Effect (-)}}\right) \frac{d \log Z}{d \tau_a} + \underbrace{\frac{1 - n_w}{1 - \beta \delta} \left(\mu \xi_{R_h}^\mu + (1 - \mu) \xi_{R_\ell}^\mu\right) \frac{d \mu}{d \tau_a}}_{\text{New! Return Innovation Effect (+)}}$$

where $\xi_x^y \equiv \frac{d \log x}{d \log Z}$ is the elasticity of variable x with respect to y.

Extensions

Extension: Infinite-Horizon Model with Mean-Reverting Productivity

- ightharpoonup Entrepreneurial productivity follows Markov process with persistence ρ (first-order autocorrelation)
- \blacktriangleright All results hold as long as entrepreneurial productivity is persistent ($\rho > 0$).

We further considered the following three extensions:

- ► Corporate sector that faces no borrowing constraint
 - If $z_{\ell} < z_{C} < z_{h}$, then low-productivity agents invest in the corporate sector.
- ► Rents: Return ≠ marginal productivity.
 - Introduce zero-sum return wedges so that $R_h <> R_\ell$.
 - Efficiency gains from $\tau_a \uparrow$ if $R_h > R_\ell$.
- ▶ Per-period entrepreneurial effort in production (still exogenous z):
 - With GHH preferences, aggregate entrepreneurial effort increases with wealth tax.





Conclusions

Increasing τ_a (& reducing τ_k):

- ightharpoonup Reallocates capital: less productive ightharpoonup more productive agents.
 - Higher TFP, output, and wages; Higher dispersion in returns and wealth
- ▶ Workers gain. High-productivity entrepreneurs gain. Low-productivity entrepreneurs (typically) lose.
- ► Equilibrium innovation increases (when innovation is endogenous).

Optimal taxes:

- ightharpoonup Optimal wealth tax increases with α .
- ▶ Optimal wealth tax is higher with endogenous innovation.

Conclusions

Increasing τ_a (& reducing τ_k):

- ► Reallocates capital: less productive → more productive agents.
- Higher TFP, output, and wages; Higher dispersion in returns and wealth
- ▶ Workers gain. High-productivity entrepreneurs gain. Low-productivity entrepreneurs (typically) lose.
- ► Equilibrium innovation increases (when innovation is endogenous).

Optimal taxes:

- ightharpoonup Optimal wealth tax increases with α .
- ▶ Optimal wealth tax is higher with endogenous innovation.

Final Remark:

- ▶ We assumed the misallocation of capital arises due to a financing constraint.
- ▶ But the source of the misallocation is not critical for the "use-it-or-lose-it" to work.
- ► Fredo might (incorrectly) believe that he is as good as Mike. [in progress]

Extra

Outline

- 1. Benchmark model with exogenous entrepreneurial productivity process
- 2. Efficiency gains from wealth taxation
- 3. Welfare effects of wealth taxation
- 4. Optimal taxation
- 5. Model with endogenous entrepreneurial productivity
- 6. Extensions
- 7. Quantitative Analysis

Entrepreneur's Problem

Financial Markets & Entrepreneurs' Production Problem

Entrepreneurs' Production Decision:

$$\Pi^{*}(z,a) = \max_{\mathbf{k} \leq \lambda a, n} (zk)^{\alpha} n^{1-\alpha} - rk - wn.$$

Financial Markets & Entrepreneurs' Production Problem

Entrepreneurs' Production Decision:

Solution:
$$\Pi^*(z, a) = \underbrace{\pi^*(z)}_{\text{Excess return above r}} \times a$$

$$\pi^{*}(z) = \begin{cases} (MPK(z) - r) \lambda & \text{if } MPK(z) > r \\ 0 & \text{otherwise.} \end{cases}$$

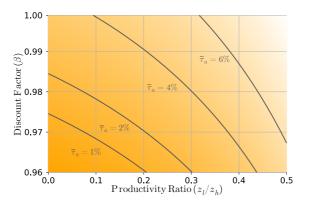
$$k^{*}(z) \begin{cases} = \lambda a & \text{if } MPK(z) > r \\ \in [0, \lambda a] & \text{if } MPK(z) = r \\ = 0 & \text{if } MPK(z) < r \end{cases}$$

 \blacktriangleright $(\lambda - 1)$ a: amount of external funds used by type-z if MPK(z) > r.

back

FIGURES

Figure 2: Upper Bound Wealth Tax

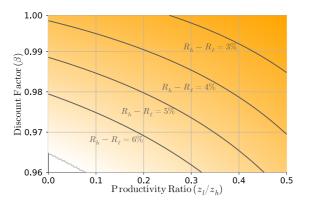


Note: The figure reports the upper bound on wealth taxes for combinations of the discount factor (β) and productivity dispersion (z_ℓ/z_h). We set the remaining parameters as follows: $\delta = 49/50$, $\beta \delta = 0.96$, $\mu = 0.10$, $z_h = 1$, $\tau_k = 25\%$, and $\alpha = 0.4$. λ is such that the debt-to-output ratio in our baseline calibration is 1.5.

Return Dispersion in Steady State of the Benchmark Economy



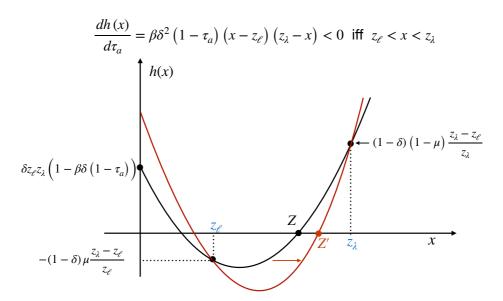




Note: The figure reports the value return dispersion in steady state for combinations of the discount factor (β) and productivity dispersion ($^{z}\ell/z_{h}$). We set the remaining parameters as follows: $\delta=49/50$, $\beta\delta=0.96$, $\mu=0.10$, $z_{h}=1$, $\tau_{k}=25\%$, and $\alpha=0.4$.

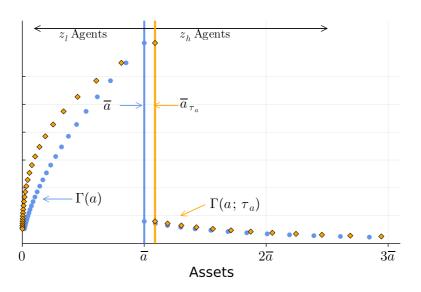
What happens to Z if $\tau_a \uparrow$?





Stationary wealth distribution and wealth taxes



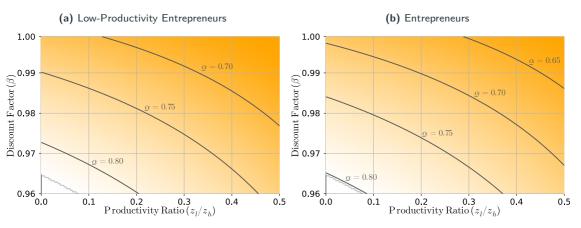


Welfare Gains

Conditions for Entrepreneurial Welfare Gain

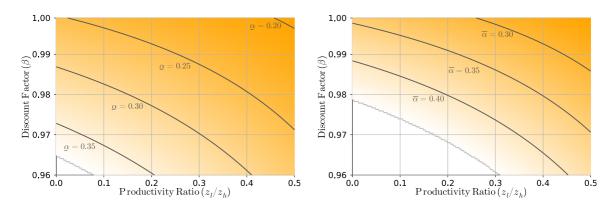


Figure 4: α Thresholds for Entrepreneurial Welfare Gains



Note: The figures report the threshold value of α above which entrepreneurial welfare increases after an increase in wealth taxes for combinations of the discount factor (β) and productivity dispersion (z_{ℓ/z_h}). We set the remaining parameters as follows: $\delta = 49/50$, $\beta \delta = 0.96$, $\mu = 0.10$, $z_h = 1$, $\tau_{\nu} = 25\%$, and $\alpha = 0.4$.

Optimal Taxes



Note: The figures report the threshold value of α for the optimal wealth taxes to be positive (left) and capital income taxes to be positive (right) for combinations of the discount factor (β) and productivity dispersion (${}^{2}\ell/z_{h}$). We set the remaining parameters as follows: $\delta={}^{49}/50$, $\beta\delta=0.96$, $\mu=0.10$, $z_{h}=1$, $\tau_{k}=25\%$, and $\alpha=0.4$.

Extensions

Extension: Corporate sector



► Corporate sector produces final goods using CRS technology:

$$Y_c = (z_c K_c)^{\alpha} L_c^{1-\alpha}$$

- No financial constraints!
- ► Corporate sector imposes lower bound on *r*:

$$r \geq \alpha z_c \left(\frac{1-\alpha}{w}\right)^{\frac{1-\alpha}{\alpha}}.$$

Interesting case: $z_{\ell} < z_{c} < z_{h}$

- ► Corporate sector and high-productivity entrepreneurs produce
- ► Low-productivity entrepreneurs lend all of their funds.
- lacktriangle No real changes in the aggregates of the economy! z_c takes the place of z_ℓ

$$Y = (ZK)^{\alpha} L^{1-\alpha}$$

but now
$$Z = s_h z_\lambda + s_l \mathbf{z_c}$$
, where $z_\lambda = z_h + (\lambda - 1)(z_h - \mathbf{z_c})$.



► Introduce wedge for returns above/below productivity:

$$R_i = (1 - \tau_a) + (1 - \tau_k) \underbrace{(1 + \omega_i)}_{\text{Return Wedge}} \alpha (Z^K/L)^{\alpha - 1} z_i$$

- ► Zero-sum condition on wedges: $\omega_I z_\ell A_\ell + \omega_h z_\lambda A_h = 0$
- lacktriangle Characterization of eq. in terms of "effective productivity" $ilde{z}_i = (1 + \omega_i) z_i$



► Introduce wedge for returns above/below productivity:

$$R_i = (1 - \tau_a) + (1 - \tau_k) \underbrace{(1 + \omega_i)}_{\text{Return Wedge}} \alpha (Z^K/L)^{\alpha - 1} z_i$$

- ► Zero-sum condition on wedges: $\omega_I z_\ell A_\ell + \omega_h z_\lambda A_h = 0$
- lacktriangle Characterization of eq. in terms of "effective productivity" $\tilde{z}_i = (1 + \omega_i) z_i$

Proposition:

For all $\tau_a < \overline{\tau}_a$, a marginal increase in wealth taxes (τ_a) increases Z, $\frac{dZ}{d\tau_a} > 0$, iff

- 1. $\rho > 0$ and $R_h > R_\ell \longrightarrow \mathsf{Same}$ mechanism as before
- 2. ρ < 0 and R_h < R \longrightarrow Reallocates wealth to the true high types next period



► Entrepreneurial production:

$$y = (zk)^{\alpha} e^{\gamma} n^{1-\alpha-\gamma} \longrightarrow e$$
: effort

- Production functions is CRS → Aggregation
- ► Entrepreneurial preferences:

$$u(c, e) = \log(c - \psi e)$$
 $\psi > 0$

- GHH preferences with no income effects Aggregation
- lacktriangledown ψ plays an important role: Cost of effort in consumption units



Problem is isomorphic to having preferences

$$u(\hat{c}) = \log \hat{c}$$
 where $\hat{c} = c - \psi e$

and modifying entrepreneurial problem to:

$$\hat{\pi}(z, k) = \max_{n, e} y - wn - rk - \underbrace{\frac{\psi}{1 - \tau_k}}_{\text{Effecive cost of effort}}$$

- ▶ Solution is just as before (linear policy functions $a^{'}$, n, and e)
- **Key:** Effective cost of effort depends on capital income tax τ_k !
 - Effort affects entrepreneurial income
 - Income subject to capital income taxes but not to **book value** wealth taxes

Extension: Entrepreneurial Effort



► Aggregate effort:

$$E = \left(\frac{(1-\tau_k)\gamma}{\psi}\right)^{\frac{1}{1-\gamma}} (ZK)^{\frac{\alpha}{1-\gamma}} L^{\frac{1-\alpha-\gamma}{1-\gamma}}$$

- Comparative statics: $K \uparrow$, $Z \uparrow$, and $\tau_k \downarrow$
- ▶ New wedge from capital income taxes on aggregate output and wages!
- lacktriangle Effort affects marginal product of capital \longrightarrow Affects K_{ss}

A neutrality result:

- ► No changes to steady state productivity!
- ► Steady state capital adjusts in background to satisfy:

$$(1- au_k)\,\mathsf{MPK}- au_{\mathsf{a}}=rac{1}{eta}-1$$

Extension: Entrepreneurial Effort



Results:

- 1. Efficiency gains from wealth taxation remain
- 2. Effect on aggregates is stronger if capital income taxes go down
 - Effort increases with wealth taxes (if $\rho > 0$)!
- 3. Characterization of optimal taxes is similar but higher wealth taxes and lower capital incomes taxes are optimal

Quantitative Framework with New Results

Model: Households



- ► **OLG** demographic structure.
- ▶ Uncertain lifetimes: individuals face mortality risk every period.
- ▶ Bequest motive, inheritance goes to (newborn) offspring.

Model: Households



- ▶ **OLG** demographic structure.
- ▶ Uncertain lifetimes: individuals face mortality risk every period.
- ▶ Bequest motive, inheritance goes to (newborn) offspring.

Individuals:

- ► Have preferences over consumption, **leisure** and bequests
- ► Make three decisions:

```
consumption-savings | labor supply | portfolio choice
```

► Two exogenous characteristics:

y_{ih} (labor market productivity) | z_{ih} (entrepreneurial productivity)

Model: Households



- ▶ **OLG** demographic structure.
- ▶ Uncertain lifetimes: individuals face mortality risk every period.
- ▶ Bequest motive, inheritance goes to (newborn) offspring.

Individuals:

- ► Have preferences over consumption, **leisure** and bequests
- ► Make three decisions:

consumption-savings | labor supply | portfolio choice

► Two exogenous characteristics:

y_{ih} (labor market productivity) | z_{ih} (entrepreneurial productivity)

Entrepreneurs: monopolistic competition \rightarrow decreasing returns to scale

Entrepreneurial Productivity z_{ih} : Key Source of Heterogeneity



- ► Idiosyncratic wage risk :
 - Modeled in a rich way, but does not turn out to be critical. Details

Entrepreneurial Productivity z_{ih} : Key Source of Heterogeneity



- ► Idiosyncratic wage risk :
 - Modeled in a rich way, but does not turn out to be critical. Details

- \triangleright Entrepreneurial productivity, z_{ih} , varies
 - 1. permanently across individuals
 - imperfectly correlated across generations
 - 2. stochastically over the life cycle

Government



Government budget balances:

- ▶ Outlays: Expenditure (G) + Social Security pensions
- **Revenues:** tax on consumption (τ_c) , labor income (τ_ℓ) , bequests (τ_b) plus:
- 1. tax on capital income (τ_k) , or
- 2. tax on wealth (τ_a) .

Calibration summary



Choose parameters of

- ► Bequest motive →
 - level and concentration of bequests

Calibration summary



Choose parameters of

- ► Bequest motive →
 - level and concentration of bequests
- ► Entrepreneurial productivity →
 - top wealth concentration (overall and in the hands of entrepreneurs)
 - shares of entrepreneurs and self-made billionaires

Calibration summary



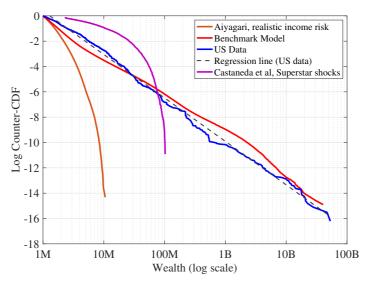
Choose parameters of

- ► Bequest motive →
 - level and concentration of bequests
- ightharpoonup Entrepreneurial productivity ightharpoonup
 - top wealth concentration (overall and in the hands of entrepreneurs)
 - shares of entrepreneurs and self-made billionaires
- ► Entrepreneurs' collateral constraint →
 - Business debt plus external funds/GDP



Pareto Tail of Wealth Distribution: Model vs. Data





Note: Both axes are in natural logs.

Performance of the benchmark model: return heterogeneity



Table 1: Distribution of Rates of Return (Untargeted) in the Model and the Data

	А	Annual Returns			Persistent Component of Returns					
	Std dev	P90-P10	Kurtosis	Std dev	P90-P10	Kurtosis	P90	P99	P99.9	
Data (Norway)	8.6	14.2	47.8	6.0	7.7	78.4	4.3	11.6*	23.4*	
Data (Norway, bus. own.)	_	_	_	4.8	10.9	14.2	10.1	-	_	
Data (US, private firms)	17.7	33.8	8.3	_	_	_	_	_	_	
Benchmark Model	8.4	17.1	7.6	4.1	9.2	6.1	5.8	13.9	19.7	
L-INEQ Calibration	6.7	13.1	9.2	3.8	9.2	4.3	5.6	11.2	15.8	

Notes: Returns on wealth in percentage points. All cross-sectional returns are value weighted. *The statistics for Norway are for individual returns on wealth (net worth) taken from Fagereng, Guiso, Malacrino, and Pistaferri (2020). The US statistics are from Smith, Zidar, and Zwick (2021) and are for S-corps' returns on investment; they also report statistics for partnerships, which are very similar (std dev of 17.8% and P90-P10 of 27.9). For each individual, the persistent component of returns is calculated following Fagereng et al as the unweighted average of annual, before-tax, returns between ages 25 and 75, after taking out the average return by age.



	$ au_k$	$ au_\ell$	$ au_{a}$	Δ Welfare
Benchmark	25%	22.4%	_	_
RN Tax reform	-	22.4%	1.19%	7.2

Opt. au_a Opt. au_k

Change in aggregate variables



	K	Q	TFP	L	Y	W	W
% change							(net)
Tax reform	16.4	22.6	2.1	1.2	9.2	8.0	8.0
Optimal $ au_{\it a}$							
Optimal τ_k				-	-		

Tax Reform: Who Gains? Who Loses?



Average (consumption equivalent) welfare gain by age-productivity groups:

	Productivity group (Percentile)							
Age	0-40	40-80	80-90	90-99	99-99.9	99.9+		
20	6.7	6.3	6.8	8.5	11.5	13.4		
21-34								
35-49								
50-64								
65+								

Tax Reform: Who Gains? Who Loses?



Average (consumption equivalent) welfare gain by age-productivity groups:

		Productivity group (Percentile)							
Age	0-40	40-80	80-90	90-99	99-99.9	99.9+			
20	6.7	6.3	6.8	8.5	11.5	13.4			
21-34	6.3	5.5	5.5	6.5	8.5	9.7			
35-49	4.9	3.8	3.3	3.3	3.1	2.8			
50-64	2.2	1.5	1.1	0.9	0.4	-0.2			
65+	-0.2	-0.3	-0.4	-0.4	-0.7	-1.0			

Tax Reform: Who Gains? Who Loses?



Average (consumption equivalent) welfare gain by age-productivity groups:

		Productivity group (Percentile)							
Age	0-40	40-80	80-90	90-99	99-99.9	99.9+			
20	6.7	6.3	6.8	8.5	11.5	13.4			
21-34	6.3	5.5	5.5	6.5	8.5	9.7			
35-49	4.9	3.8	3.3	3.3	3.1	2.8			
50-64	2.2	1.5	1.1	0.9	0.4	-0.2			
65+	-0.2	-0.3	-0.4	-0.4	-0.7	-1.0			

BB tax reform turns welfare losses of retirees to gains, ranging from 2.3% to 6.5%.



	$ au_k$	$ au_\ell$	$ au_{a}$	Δ Welfare
Benchmark	25%	22.4%	_	_
RN Tax reform	_	22.4%	1.19%	7.2
Opt. τ_a				
Opt. $ au_k$				



	$ au_k$	$ au_\ell$	$ au_{a}$	ΔWelfare
Benchmark	25%	22.4%	_	_
RN Tax reform	_	22.4%	1.19%	7.2
Opt. $ au_a$	-	15.4%	3.03%	8.7
Opt. τ_k				



	$ au_k$	$ au_\ell$	$ au_{a}$	ΔWelfare
Benchmark	25%	22.4%	_	_
RN Tax reform	_	22.4%	1.19%	7.2
Opt. $ au_a$	_	15.4%	3.03%	8.7
Opt. $ au_k$	-13.6%	31.2%	-	5.1

Change in aggregate variables



	K	Q	TFP	L	Y	W	W
% change							(net)
Tax reform	16.4	22.6	2.1	1.2	9.2	8.0	8.0
Optimal $ au_{\it a}$	2.6	10.5	3.1	3.3	6.1	2.8	12.0
Optimal τ_k							

Change in aggregate variables



	K	Q	TFP	L	Y	W	W
% change							(net)
Tax reform	16.4	22.6	2.1	1.2	9.2	8.0	8.0
Optimal $ au_{\it a}$	2.6	10.5	3.1	3.3	6.1	2.8	12.0
Optimal τ_k	38.6	46.1	2.2	-1.0	15.7	16.8	3.6



Welfare gain comes from changes in consumption (c) and leisure (ℓ) .



Welfare gain comes from changes in consumption (c) and leisure (ℓ) .

	Tax Reform	$Opt. au_k$	$Opt. au_{a}$
CE_2 (NB)	7.2	5.1	8.7
Level $(\overline{c}, \overline{\ell})$	8.9		
Dist. (c, ℓ)	-1.5		



Welfare gain comes from changes in consumption (c) and leisure(ℓ).

	Tax Reform	$Opt. au_k$	$Opt. au_{a}$
CE ₂ (NB)	7.2	5.1	8.7
Level $(\overline{c}, \overline{\ell})$	8.9	14.7	
Dist. (c, ℓ)	-1.5	-8.3	



Welfare gain comes from changes in consumption (c) and leisure(ℓ).

	Tax Reform	$Opt. au_k$	$Opt. au_{a}$
CE ₂ (NB)	7.2	5.1	8.7
Level $(\overline{c}, \overline{\ell})$	8.9	14.7	5.9
Dist. (c, ℓ)	-1.5	-8.3	2.6

Optimal taxes with transition

Optimal Tax Equilibrium with Transition



- ▶ Fix opt. tax level $(\tau_k \text{ or } \tau_a)$ and solve transition to new steady state
- lackbox Use labor income tax (au_ℓ) to finance debt from deficits during transition

Optimal Tax Equilibrium with Transition



- ▶ Fix opt. tax level $(\tau_k \text{ or } \tau_a)$ and solve transition to new steady state
- Use labor income tax (τ_{ℓ}) to finance debt from deficits during transition

	$ au_k$ Transition	$ au_a$ Transition
$ au_k$	-13.6*	0.00
$ au_{a}$	0.00	3.03^{*}
$ au_\ell$	39.90	17.01
$\overline{\textit{CE}}_2$ (newborn)	-8.4 (5.1)	6.0 (8.7)
$\overline{\textit{CE}}_2$ (all)	-6.1 (4.5)	3.5 (4.3)